

# ENTERTAINMENT RIGGING SESSIONS

Math Workbook

V2.7.19



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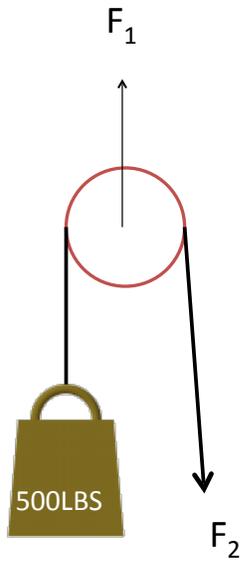


<http://files.entertainmentriggingsessions.com/>



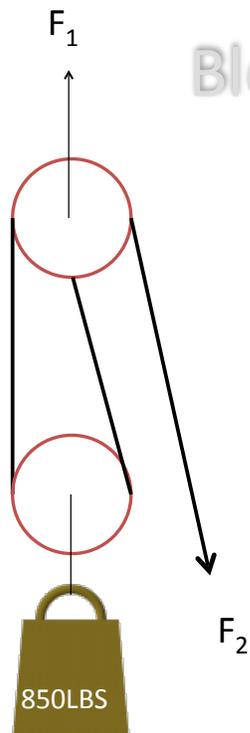
# Block and Fall

$$F_1 = \frac{\text{NumberOfLinesOnStandingBlock}}{\text{NumberofLinesonRunningBlock}} (FA)$$



# Block and Fall

$$F_1 = \frac{\text{NumberOfLinesOnStandingBlock}}{\text{NumberofLinesonRunningBlock}} (FA)$$



# Wind Loads

Wind Speed MPH	10	20	30	40	50	60	70	80	90	100	110	120	130
Wind Pressure (Q <sub>s</sub> )	.03	1.0	2.3	4.3	6.5	9.3	12.6	16.4	20.8	25.6	31	36.9	43.3

Height in Feet	Exposure Coefficient C <sub>E</sub>	
	Average Location	Location Near Large Body of Water
15	1.06	1.39
20	1.13	1.45
25	1.19	1.50
30	1.23	1.54
40	1.31	1.62
60	1.43	1.73

$WindForce =$   
 $P = (1.4)(Q_S)(C_E)(AREA)$



# Wind Loads

- 10' tall by 30' wide banner on a truss goalpost.
- Top edge at 25' from the ground.
- The wind is gusting at 40 MPH.

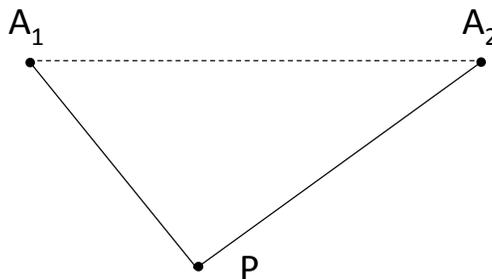


# Standard Definitions

## Reference points

- **A(n)** = Anchorage (n is the anchorage number)
- **P** = The point at which the force is applied
- **O** = The origin of a force vector
- **T** = The termination of a force vector

# Standard Definitions



# Standard Definitions

## Distances

- **S** = The horizontal distance between anchorages. This distance is also commonly referred to as **Span**.
- **D(n)** = The horizontal distance from anchorage (n), where (n) is the anchorage number, to the applied force. This form is only used when all distances are horizontal.
- **DV** = The vertical distance between the anchorages of a bridle and the bridle point. This form can only be used when all anchorages are at the same height.
- **DZ** = An alternative to **DV**. Used if the Cartesian coordinate system is being used to describe points.



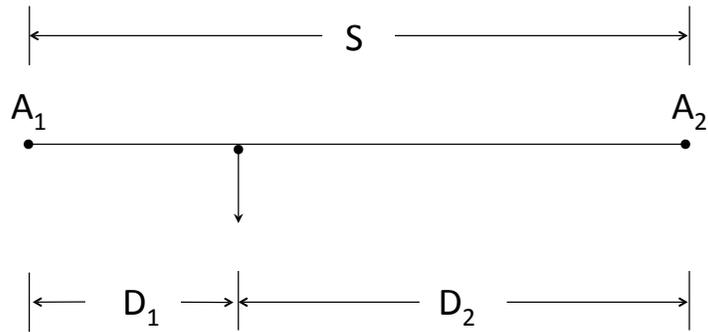
# Standard Definitions

## Distances

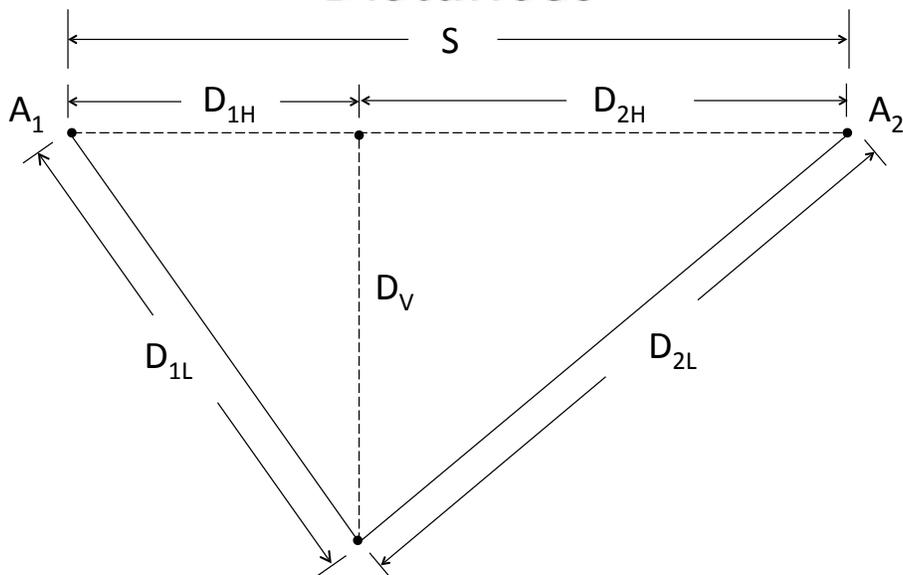
- **D(n)(x)** = The distance from anchorage (n), where (n) is the anchorage number, to the applied force in the direction (x). The direction (x) would be one of the following:
  - **H** = Horizontal in-line with the bridle leg
  - **V** = Vertical
  - **X** = In the x-axis
  - **Y** = In the y-axis
  - **Z** = In the z-axis
  - **L** = In-line with the bridle leg



# Standard Definitions Distances



# Standard Definitions Distances



# Standard Definitions

## Forces

- **FA** = The applied force
- **FA(x)** = A component of the applied force in the direction (**x**).
  - The direction (**x**) would be one of the following:
    - **H** = Horizontal in-line with the applied force
    - **V** = Vertical
    - **X** = In the x-axis
    - **Y** = In the y-axis
    - **Z** = In the z-axis



# Standard Definitions

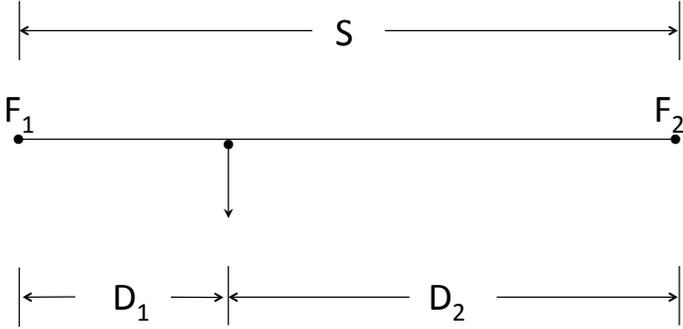
## Forces

- **F(n)** = The vertical force at anchorage (n), where (n) is the anchorage number. This form is used only when all forces being analyzed are vertical.
- **F(n)(x)** = The force at anchorage (n), where (n) is the anchorage number, in the direction (x). The direction (x) would be one of the following:
  - **L** = In-line with the bridle leg
  - **H** = Horizontal in-line with the bridle leg
  - **V** = Vertical
  - **X** = In the x-axis
  - **Y** = In the y-axis
  - **Z** = In the z-axis



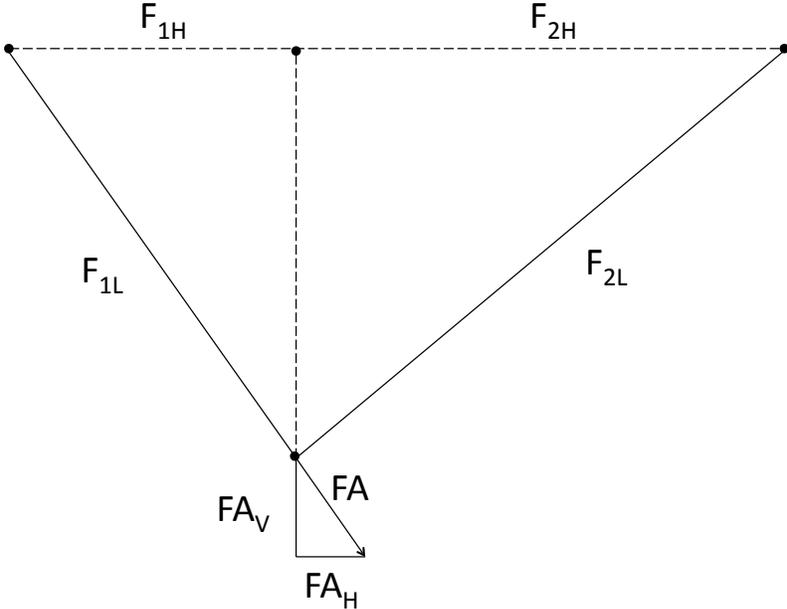
# Standard Definitions

## Forces



# Standard Definitions

## Forces



# Standard Definitions

## Angles

- $\alpha(n)$  = The angle between the bridle leg and horizontal at point
- $A(n)$ , where  $(n)$  is the anchorage number.
- $\alpha(n)r$  = The angle of rotation of the bridle leg around  $A(n)$ , where  $(n)$  is the anchorage number.
- $p(n)$  = The angle between the anchorage and vertical at point  $P$ , where  $(n)$  is the anchorage number.
- $p$  = the angle between the bridle legs with a base at  $P$ .
- $o$  = The acute angle between  $FA$  and horizontal with a base at  $O$ .
- $or$  = The angle of rotation of the force around  $O$ .
- $t$  = The acute angle between  $FA$  and vertical with a base at  $T$ .



# Order of Operation

## PEMDAS

- Rule 1:** First perform any calculations inside parentheses.
- Rule 2:** Next perform all exponents, working from left to right.
- Rule 3:** Next perform all multiplications and divisions, working from left to right.
- Rule 4:** Lastly, perform all additions and subtractions, working from left to right.



## Order of Operation

$$7 \times 2 + (7 + 3 \times (5 - 2)) \div 4 \times 2$$

## Basic Engineering Principles

### *Newton's First Law*

*Every body persists in its state of being at rest or of moving uniformly straight forward, except insofar as it is compelled to change its state by force impressed*

# Basic Engineering Principles

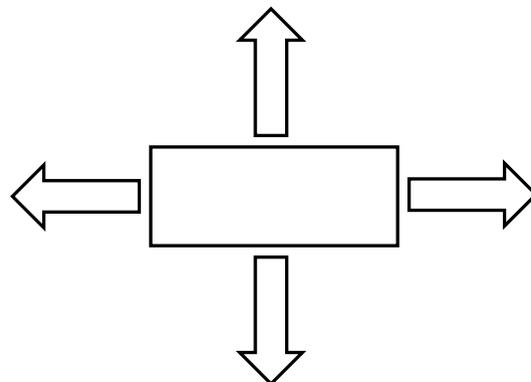
## *Newton's First Law*

An object that is at rest will stay at rest unless an unbalanced force acts upon it.



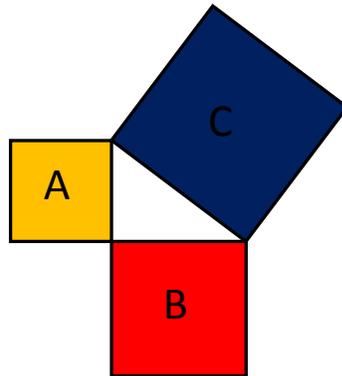
# Basic Engineering Principles

Equilibrium of forces



# Basic Engineering Principles

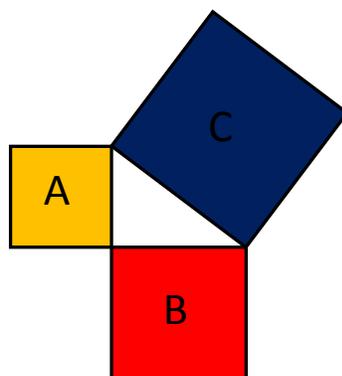
Pythagorean Theorem



The area of Square A plus the area of Square B is equal to that of the area of Square C

# Basic Engineering Principles

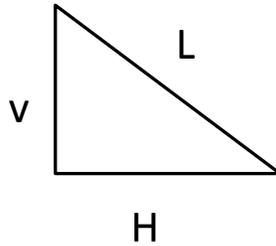
Pythagorean Theorem



$$A^2 + B^2 = C^2$$

# Basic Engineering Principles

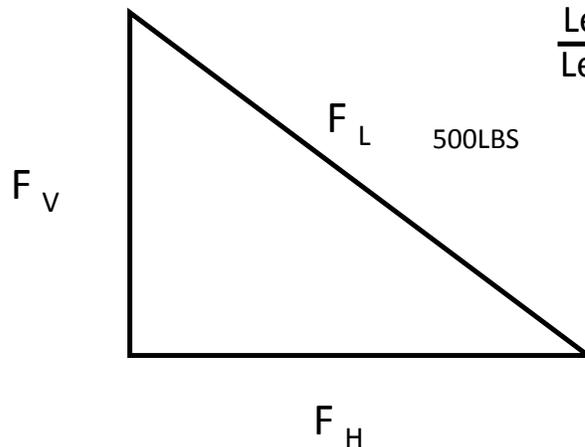
Pythagorean Theorem



$$V^2 + H^2 = L^2$$

# Basic Engineering Principles

Equal Ratios



$$\frac{\text{Length } L}{\text{Length } H} = \frac{\text{Force } L}{\text{Force } H}$$

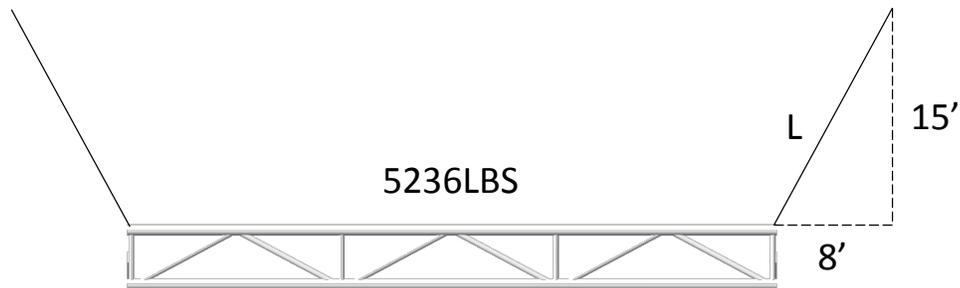
# Basic Engineering Principles

$$\frac{\text{Force L}}{\text{Force V}} = \frac{\text{Length L}}{\text{Length V}}$$

# Basic Engineering Principles

$$\text{Force L} = \frac{\text{Length L}}{\text{Length V}} (\text{Force V})$$

# Basic Engineering Principles



What is the Length of L?  
What is the Force on L?

## Point Loads

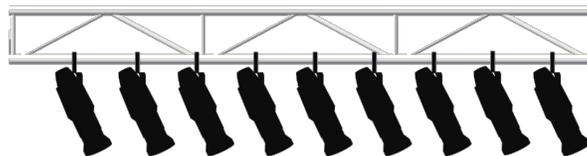
- A single concentrated load on a truss, batten, Etc.
  - Moving Lights
  - Projectors
  - Audio
  - Other rigging
- Know as PL

# Uniformly Distributed Loads

- Multiple point loads that are evenly spaced along a span
  - Lighting Fixtures
  - Truss Self Weight
  - Cable
  - Drape
- Know as UDL

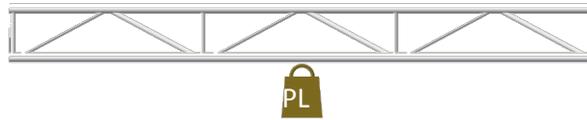
# Uniformly Distributed Loads

UDL

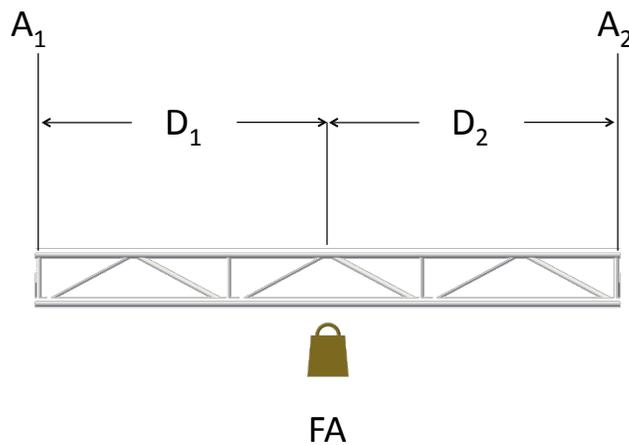


# Uniformly Distributed Loads

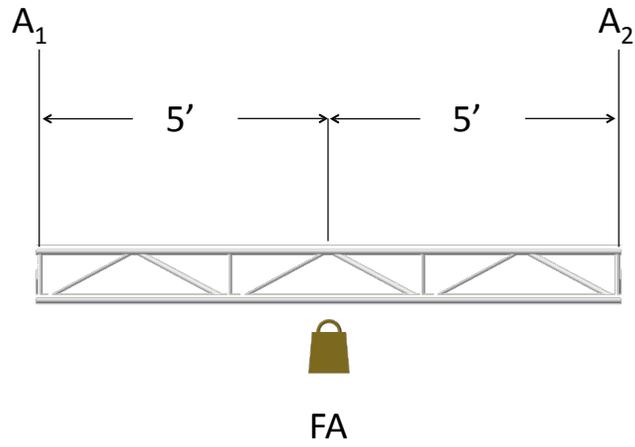
UDL can be treated as a PL centered between the suspensions



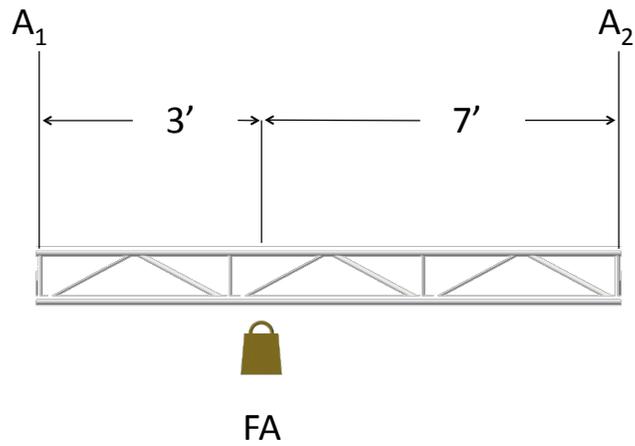
# Simple Span



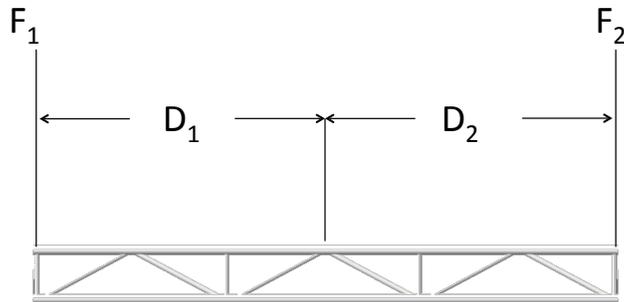
# Simple Span



# Simple Span



# Simple Span

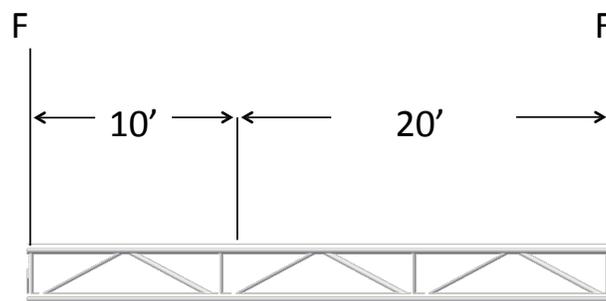


$$F_1 = (FA) \frac{D_2}{S}$$

$FA$

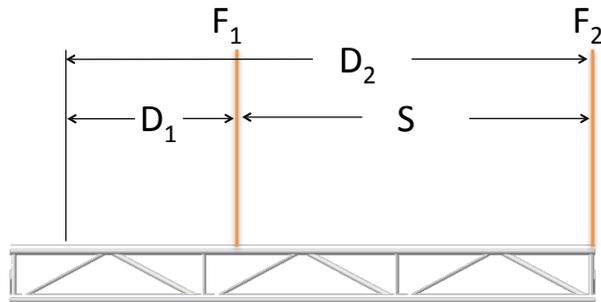
$$F_2 = \frac{(FA)(D_1)}{S}$$

# Simple Span



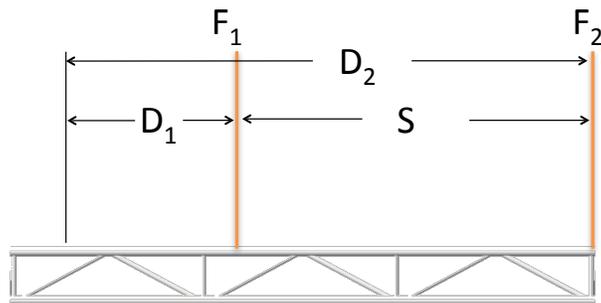
$750LBS$

# Cantilevers



$$F_1 = \frac{(FA)(D_2)}{S}$$

# Cantilevers



$$F_2 = \frac{-(FA)(D_1)}{S}$$

# Cantilevers

The total weight to be placed on the cantilevered truss must be Less than the allowable CPL for a span (4) times the length of the Cantilever.



# Cantilevers

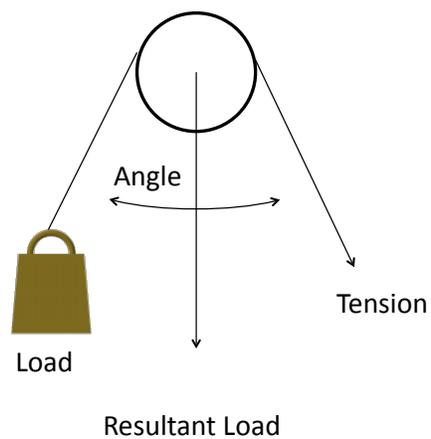
span (ft)	Uniform Loads			Center Pt. Load		Third Pt. Load		Quarter Pt. Load	
	load (plf)	load (lbs)	defl (in)	load (lbs)	defl (in)	load (lbs)	defl (in)	load (lbs)	defl (in)
5	817	4085	0.016	2398	0.015	1199	0.012	1182	0.017
10	406	4060	0.124	2372	0.116	1186	0.099	1174	0.136
15	262	3930	0.409	1965	0.329	1173	0.334	982	0.389
20	145	2903	0.727	1451	0.587	1089	0.743	726	0.692
25	91	2276	1.136	1138	0.921	854	1.160	569	1.083
30	62	1850	1.636	925	1.334	694	1.670	463	1.561
35	44	1538	2.227	769	1.828	577	2.272	385	2.127
40	24	950	2.235	475	1.867	356	2.276	238	2.143



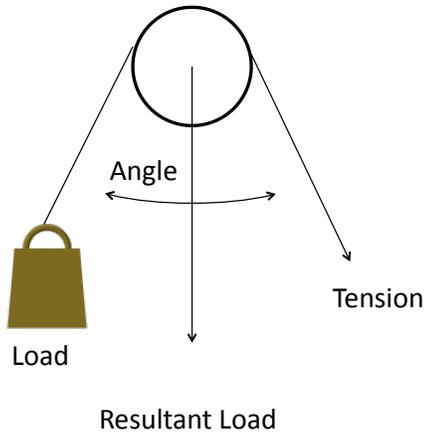
# Resultant Loads

What is a Resultant load?

# Resultant Loads



# Resultant Loads



2 ways to determine the Resultant Load

Use a multiplying Factor

Use Trigonometry



# Resultant Loads

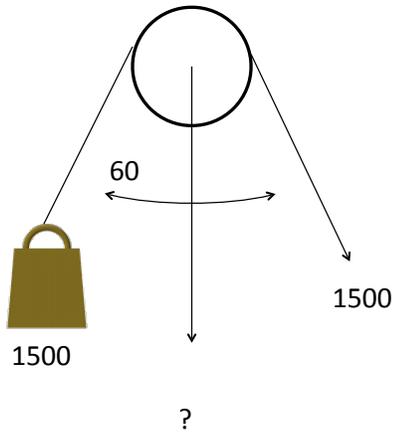
Angle	Multiplying Factor	Angle	Multiplying Factor
0	2.00	100	1.29
10	1.99	110	1.15
20	1.97	120	1.00
30	1.93	130	0.85
40	1.88	140	0.68
50	1.81	150	0.52
60	1.73	160	0.35
70	1.64	170	0.17
80	1.53	180	0.00
90	1.41		

2 ways to determine the Resultant Load

Resultant Load = (Force) (Multiplying Factor)



# Resultant Loads



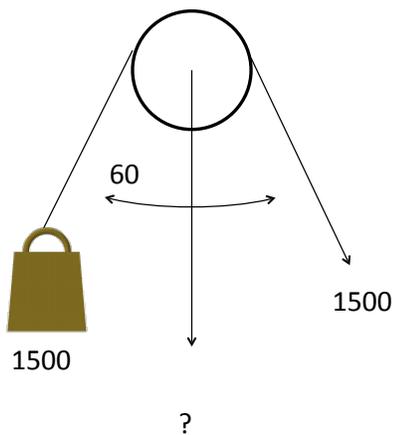
Angle	Multiplying Factor
60	1.73

$$\text{Resultant Load} = (1500)(1.73)$$

$$\text{Resultant Load} = 2595$$



# Resultant Loads

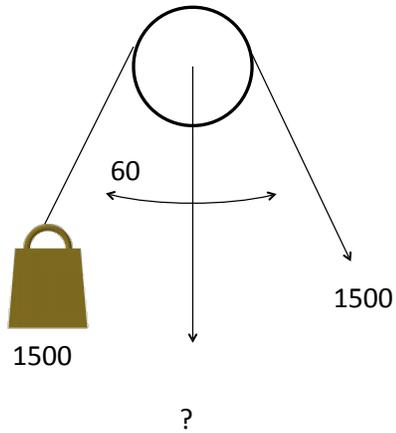


Trigonometry

$$\text{Resistant Load} = \frac{(FA)(\sin(\text{Angle}))}{\sin\left(\frac{\text{Angle}}{2}\right)}$$



# Resultant Loads



Trigonometry

$$\frac{(1500)(\sin(60))}{\sin(\frac{60}{2})}$$

$$\frac{(1500)(.866)}{\sin 30}$$

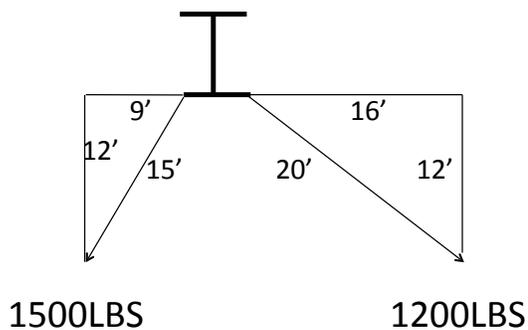
$$\frac{1299}{0.5}$$

Resultant Load = 2598



# Resultant Loads

Using Resultants to figure out loads on beams



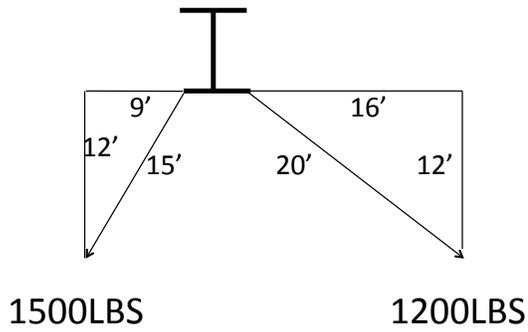
1. Figure out Horizontal Forces
2. Figure Out Vertical Forces
3. Add (or Subtract) Horizontal forces
4. Add (or Subtract) Vertical forces
5. Using the Pythagorean Theorem, Find the Resultant Load



# Resultant Loads

Using Resultants to figure out loads on beams

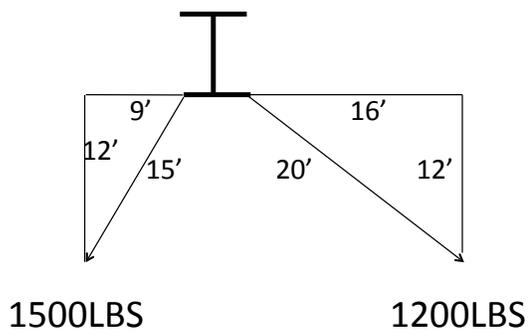
$$F_H = \left(\frac{D_H}{D_L}\right)(F A)$$



# Resultant Loads

Using Resultants to figure out loads on beams

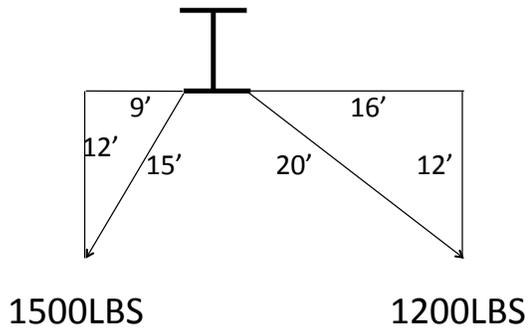
$$F_H = \left(\frac{D_H}{D_L}\right)(F A)$$



# Resultant Loads

Using Resultants to figure out loads on beams

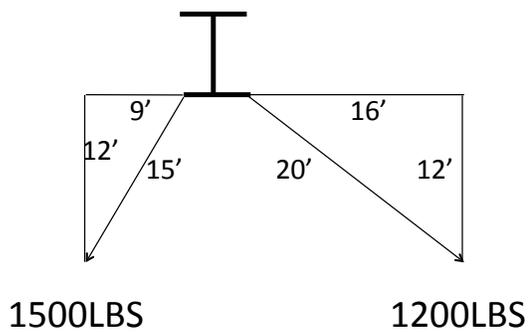
$$F_V = \left(\frac{D_V}{D_L}\right)(FA)$$



# Resultant Loads

Using Resultants to figure out loads on beams

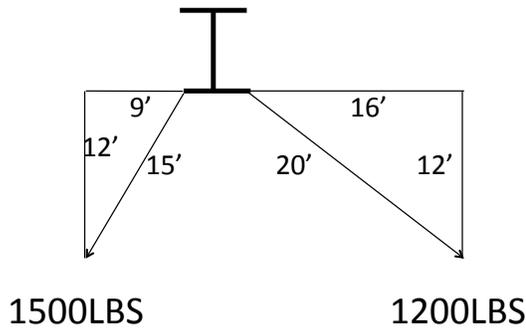
$$F_V = \left(\frac{D_V}{D_L}\right)(FA)$$



# Resultant Loads

Using Resultants to figure out loads on beams

Slope of Resultant Force

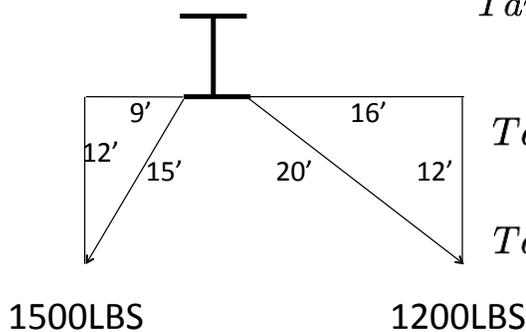


$$\frac{F_H}{F_V}$$



# Resultant Loads

Using Resultants to figure out loads on beams



$$\tan(\text{Resultant Angle}) = \frac{\text{Total } F_H}{\text{Total } F_V}$$

$$\tan(\text{Resultant Angle}) = \frac{60}{1920}$$

$$\tan(\text{Resultant Angle}) = 0.03125$$

$$\text{Resultant Angle} = \arctan(0.03125)$$

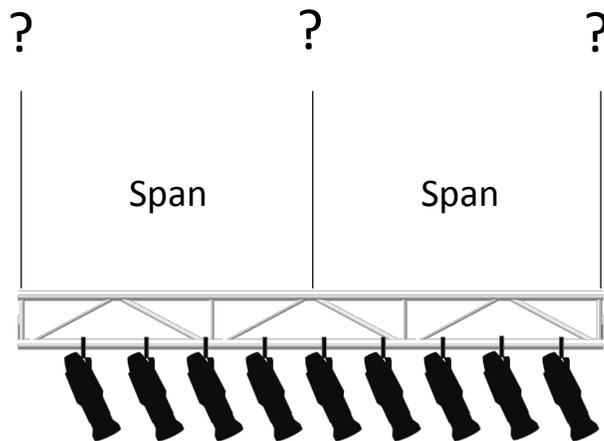
$$\text{Resultant Angle} = 1.790^\circ$$



# Complex Structures

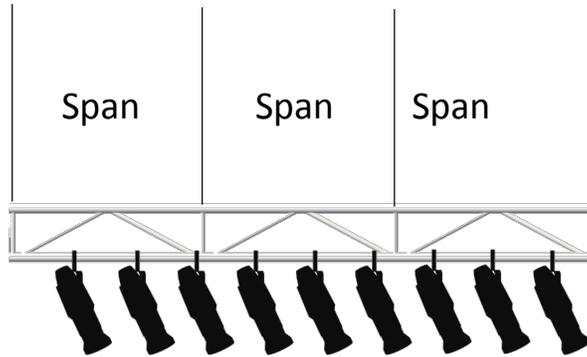
What happens when we add a suspension point?

# Complex Structures



# Complex Structures

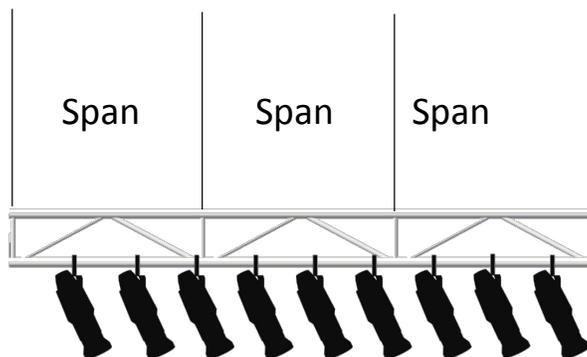
.5 Span    Span + 14%    Span + 14%    .5 Span



# Complex Structures

Mathematically the loads are different

.4 Span    1.1 Span    1.1 Span    .4 Span



# Complex Structures

So why not just use the Mathematical solution?

The process for calculating the loads uses the Three Moment Theorem, which is not very practical in the field due to the complexity of the math



# Complex Structures

Use a “Rule of Thumb”

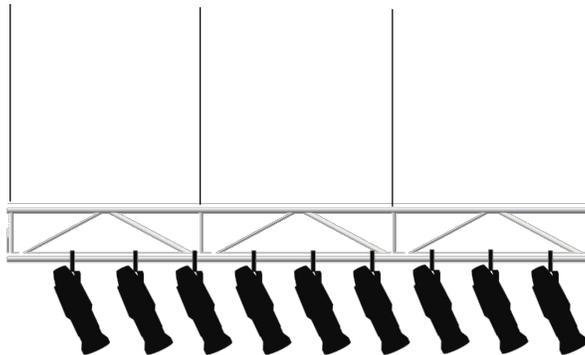
Harry Donovan figured out that the biggest difference between intuition and the mathematically correct answer on a structure with 3 suspensions is 25% and a structure with 4 or more suspensions is 14%



# Complex Structures

Rule of Thumb for 4 or more suspensions

.5 Span    Span + 14%    Span + 14%    .5 Span



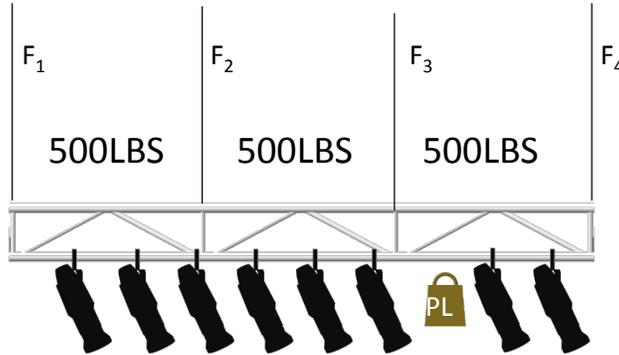
# Complex Structures

What happens when we add a Point Load?

We can use the simple span equation in combination with the “Rule of Thumb”

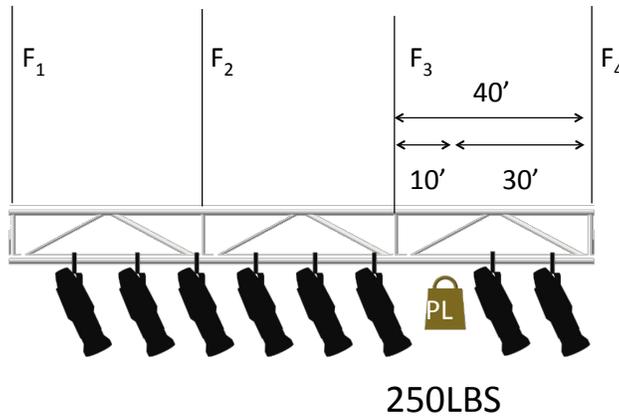
# Complex Structures

.5 Span    Span + 14%    Span + 14%    .5 Span

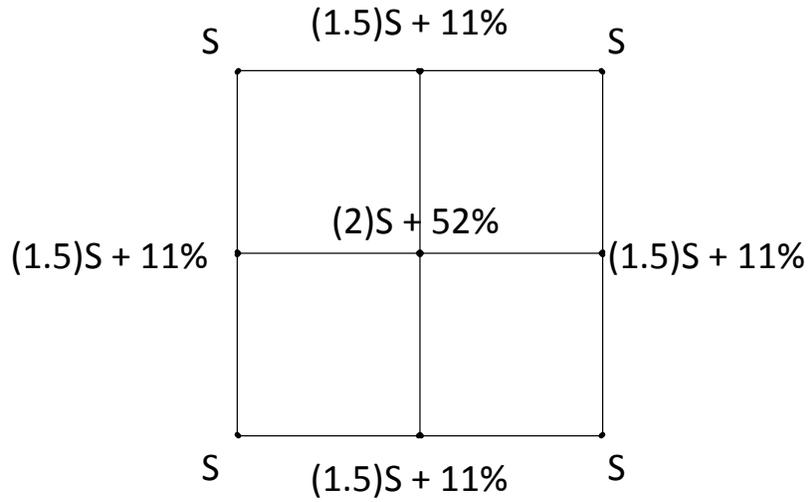


# Complex Structures

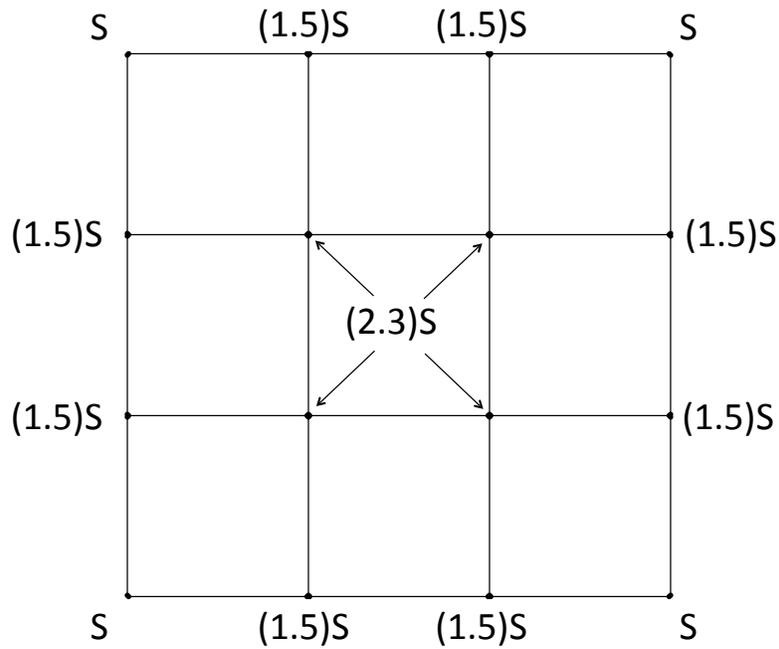
.5 Span    Span + 14%    Span + 14%    .5 Span



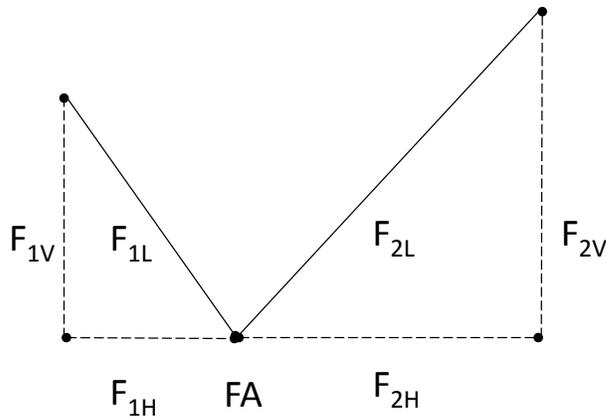
# Complex Structures



# Complex Structures



## Math Solutions to Simple Bridles



$$F_{1L} = \frac{(FA)D_{2H}D_{1L}}{D_{1V}D_{2H} + D_{2V}D_{1H}}$$

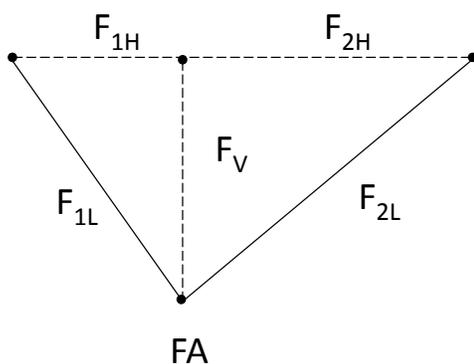
$$F_{2L} = \frac{(FA)D_{1H}D_{2L}}{D_{1V}D_{2H} + D_{2V}D_{1H}}$$

$$F_{1V} = \frac{(FA)D_{2H}D_{1V}}{D_{1V}D_{2H} + D_{2V}D_{1H}}$$

$$F_{2V} = \frac{(FA)D_{1H}D_{2V}}{D_{1V}D_{2H} + D_{2V}D_{1H}}$$

$$F_H = \frac{(FA)D_{1H}D_{2H}}{D_{1V}D_{2H} + D_{2V}D_{1H}}$$

## Math Solutions to Simple Bridles



If the beams are at the same height you can simplify the equation

$$F_{1L} = \frac{(FA)D_{2H}D_{1L}}{D_V(\text{Span})}$$

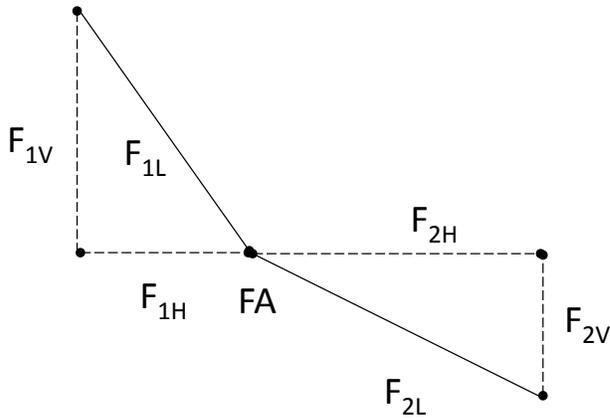
$$F_{2L} = \frac{(FA)D_{1H}D_{2L}}{D_V(\text{Span})}$$

$$F_{1V} = \frac{(FA)D_{2H}}{D_V(\text{Span})}$$

$$F_{2V} = \frac{(FA)D_{1H}}{D_V(\text{Span})}$$

$$F_H = \frac{(FA)D_{1H}D_{2H}}{D_V(\text{Span})}$$

# Math Solutions to Simple Bridles



If one beam is BELOW the junction

$$F_{1L} = \frac{(FA)D_{2H}D_{1L}}{D_{1V}D_{2H} - D_{2V}D_{1H}}$$

$$F_{2L} = \frac{(FA)D_{1H}D_{2L}}{D_{1V}D_{2H} - D_{2V}D_{1H}}$$

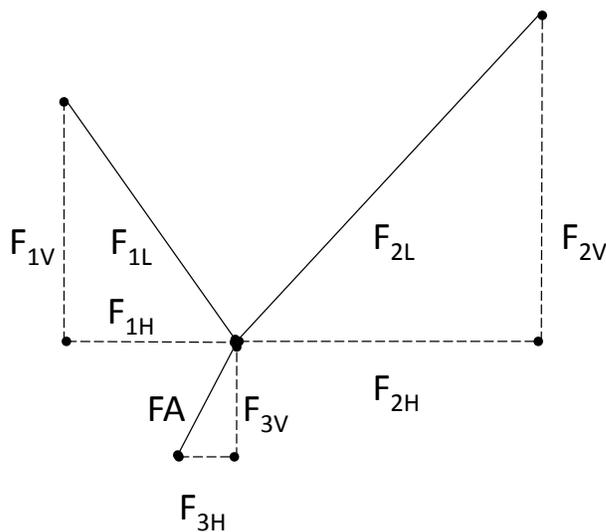
$$F_{1V} = \frac{(FA)D_{2H}D_{1V}}{D_{1V}D_{2H} - D_{2V}D_{1H}}$$

$$F_{2V} = \frac{(FA)D_{1H}D_{2V}}{D_{1V}D_{2H} - D_{2V}D_{1H}}$$

$$F_H = \frac{(FA)D_{1H}D_{2H}}{D_{1V}D_{2H} - D_{2V}D_{1H}}$$



# Math Solutions to Simple Bridles



$$F_{1L} = FA \left( \frac{D_{1L}}{D_{3L}} \right) \left( \frac{D_{3V}D_{2H} - D_{2V}D_{3H}}{D_{1V}D_{2H} - D_{2V}D_{1H}} \right)$$

$$F_{2L} = FA \left( \frac{D_{2L}}{D_{3L}} \right) \left( \frac{D_{3V}D_{1H} - D_{1V}D_{3H}}{D_{1V}D_{2H} - D_{2V}D_{1H}} \right)$$

$$F_{1V} = (F_{1L}) \left( \frac{D_{1V}}{D_{1L}} \right)$$

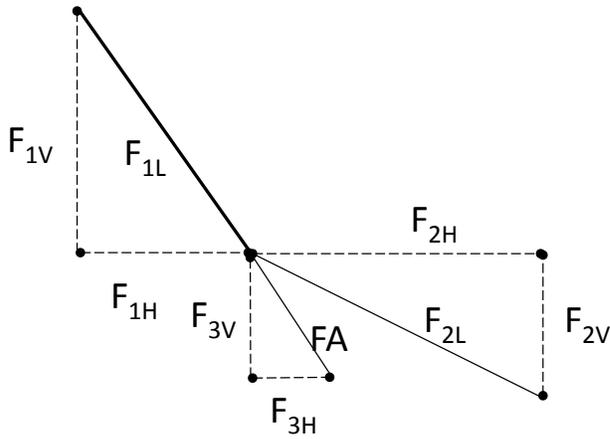
$$F_{2V} = (F_{2L}) \left( \frac{D_{2V}}{D_{2L}} \right)$$

$$F_{1H} = (F_{2L}) \left( \frac{D_{1H}}{D_{1L}} \right)$$

$$F_{2H} = (F_{2L}) \left( \frac{D_{2H}}{D_{2L}} \right)$$



# Math Solutions to Simple Bridles



$$F_{1L} = D_{1L} \left( \frac{F_{3V} D_{2H} - F_{3H} D_{2V}}{D_{1V} D_{2H} - D_{2V} D_{1H}} \right)$$

$$F_{2L} = D_{2L} \left( \frac{F_{3V} D_{1H} - F_{3H} D_{1V}}{D_{1V} D_{2H} - D_{2V} D_{1H}} \right)$$

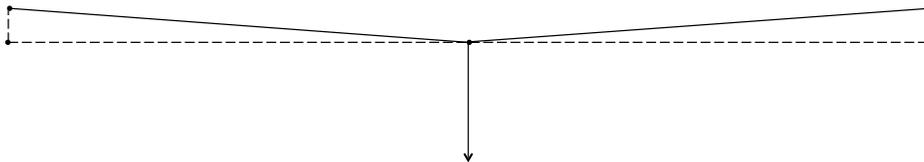


# Math Solutions to Simple Bridles

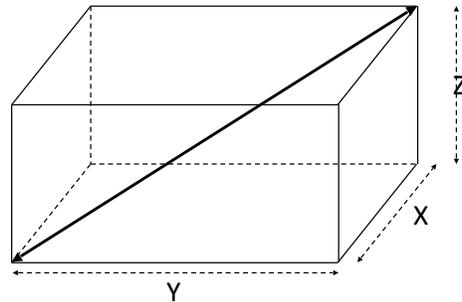
2 Workers on this horizontal lift line.

40'

Deflection = 1/20 of span

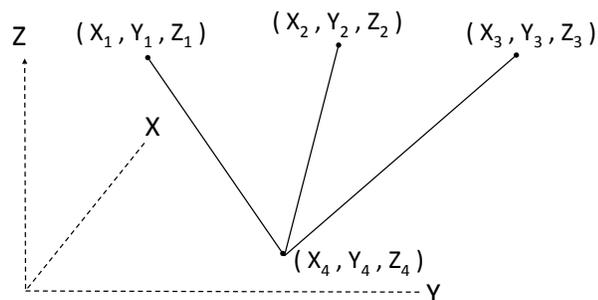


## 3 leg Bridles



$$L = \sqrt{X^2 + Y^2 + Z^2}$$

## 3 leg Bridles



$$L_1 = \sqrt{(X_1 - X_4)^2 + (Y_1 - Y_4)^2 + (Z_1 - Z_4)^2}$$

$$L_2 = \sqrt{(X_2 - X_4)^2 + (Y_2 - Y_4)^2 + (Z_2 - Z_4)^2}$$

$$L_3 = \sqrt{(X_3 - X_4)^2 + (Y_3 - Y_4)^2 + (Z_3 - Z_4)^2}$$

## 3 leg Bridles

$$N_{1X} = \frac{X_1 - X_4}{L_1} \quad N_{1Y} = \frac{Y_1 - Y_4}{L_1} \quad N_{1Z} = \frac{Z_1 - Z_4}{L_1}$$

$$N_{2X} = \frac{X_2 - X_4}{L_2} \quad N_{2Y} = \frac{Y_2 - Y_4}{L_2} \quad N_{2Z} = \frac{Z_2 - Z_4}{L_2}$$

$$N_{3X} = \frac{X_3 - X_4}{L_3} \quad N_{3Y} = \frac{Y_3 - Y_4}{L_3} \quad N_{3Z} = \frac{Z_3 - Z_4}{L_3}$$



## 3 leg Bridles

$$D = (N_{1X})(N_{2Y})(N_{3Z}) + (N_{2X})(N_{3Y})(N_{1Z}) + (N_{1Y})(N_{2Z})(N_{3X}) \\ - (N_{3X})(N_{2Y})(N_{1Z}) - (N_{3Y})(N_{2Z})(N_{1X}) - (N_{2X})(N_{1Y})(N_{3Z})$$



## 3 leg Bridles

$$F_1L = ((N_{2X})(N_{3Y}) - (N_{3X})(N_{2Y}))\left(\frac{FA}{D}\right)$$

$$F_2L = ((N_{3X})(N_{1Y}) - (N_{1X})(N_{3Y}))\left(\frac{FA}{D}\right)$$

$$F_3L = ((N_{1X})(N_{2Y}) - (N_{2X})(N_{1Y}))\left(\frac{FA}{D}\right)$$

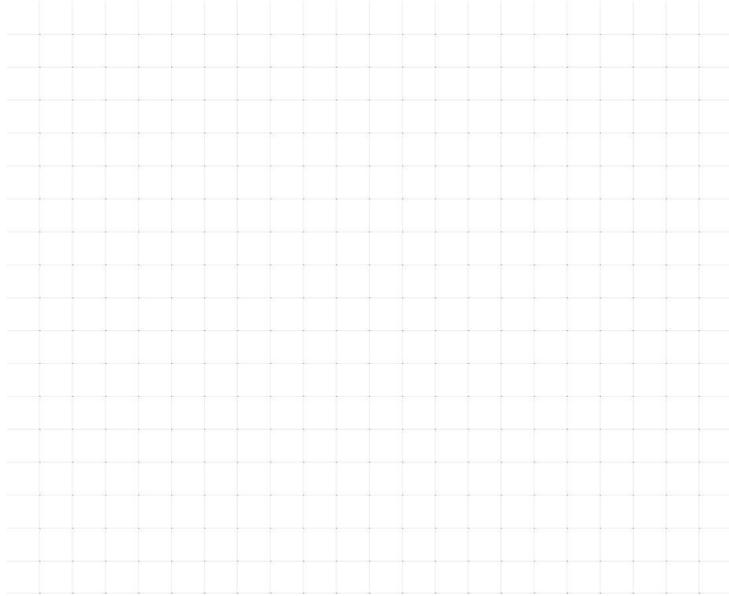


## Vector Solutions to Simple Bridles

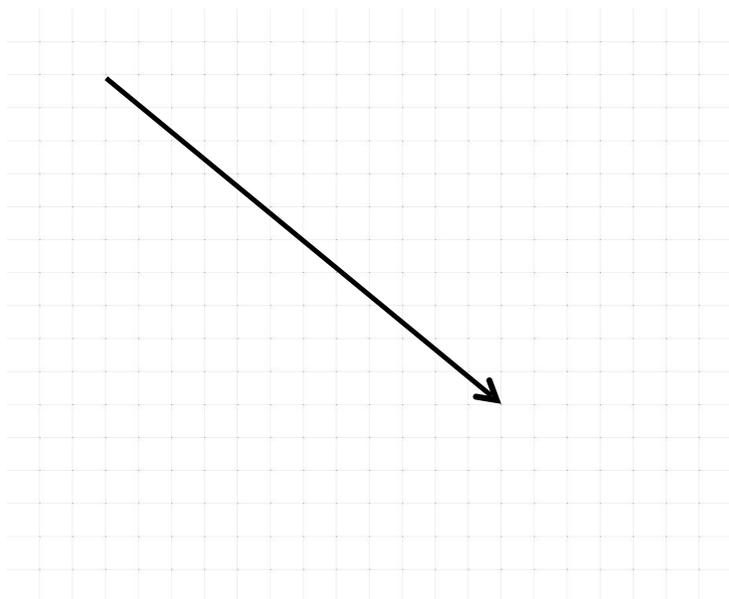
- Vectors offer an alternative to Algebra
- Helps to visualize the forces
- Slower to calculate loads
- Not as Accurate



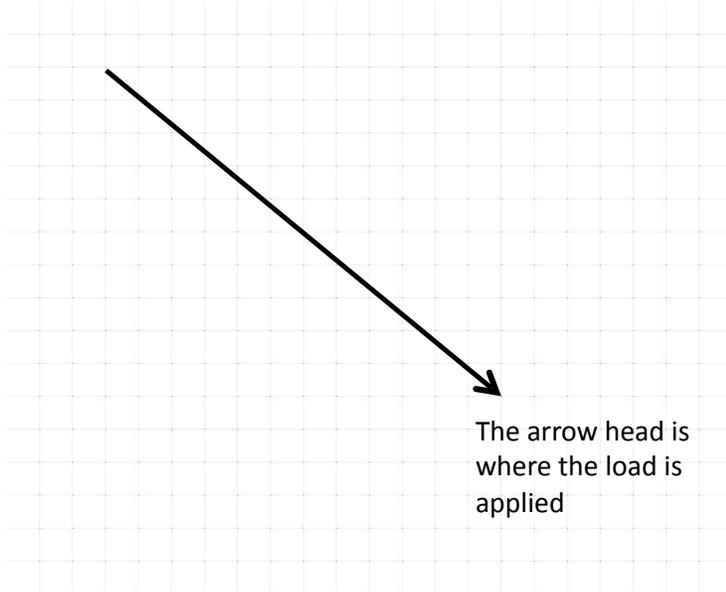
# Vectors



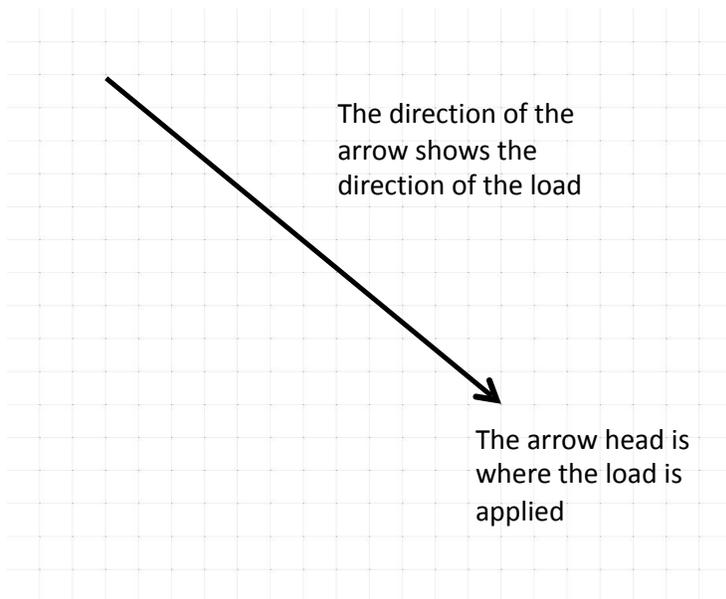
# Vectors



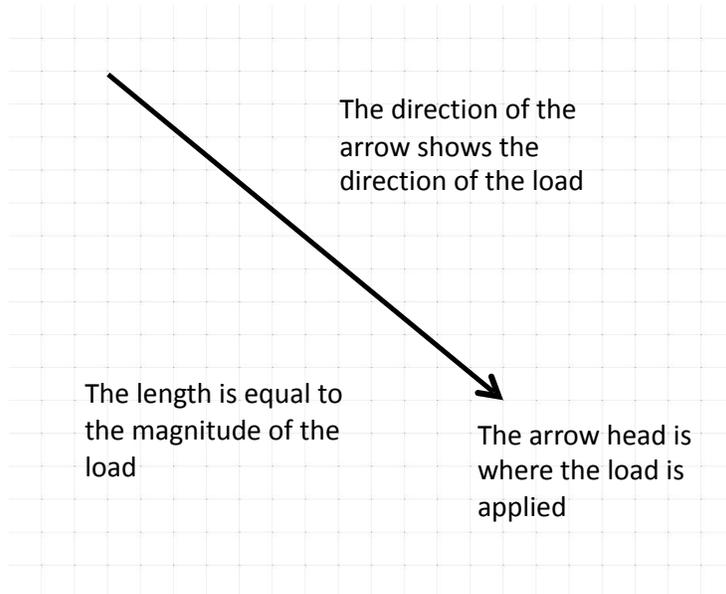
# Vectors



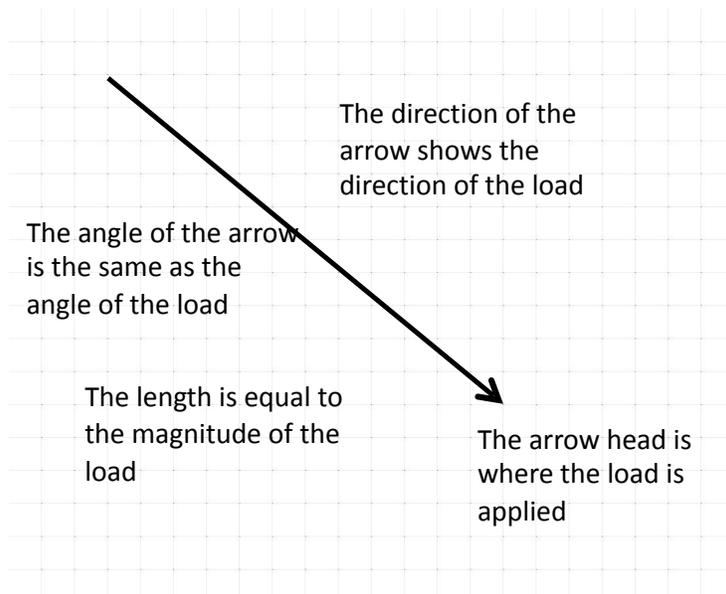
# Vectors



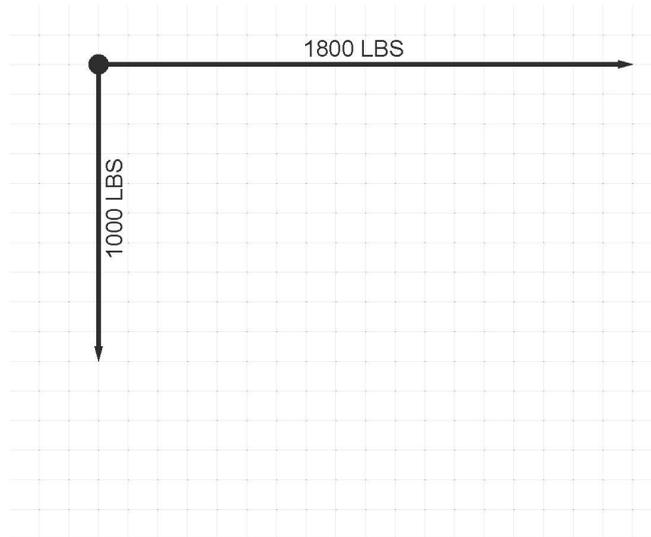
# Vectors



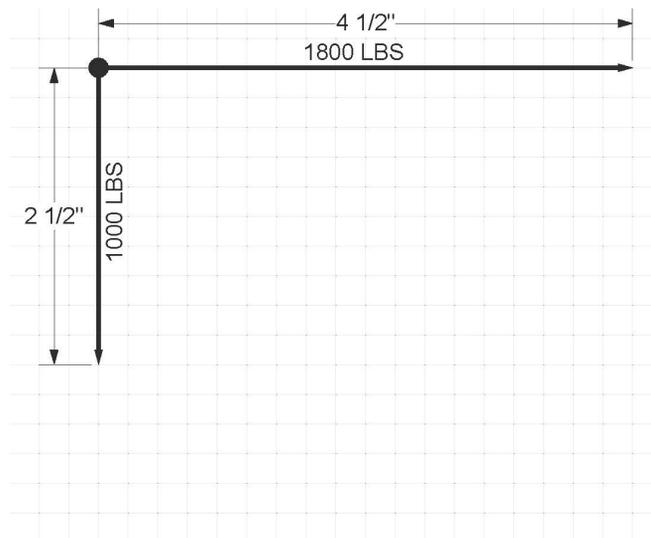
# Vectors



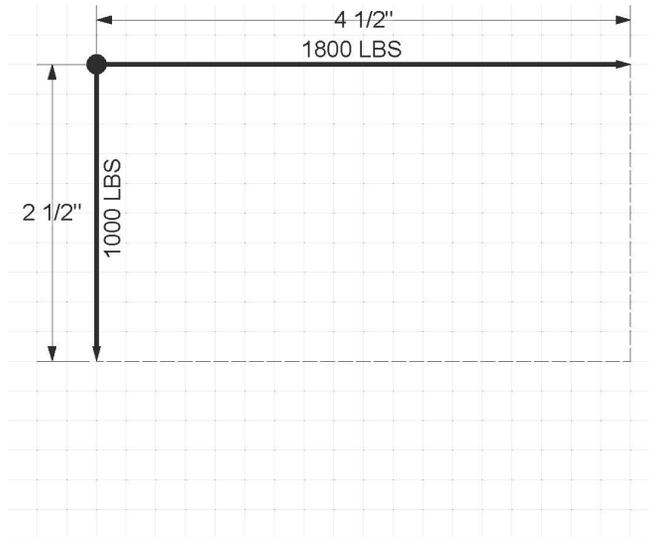
# Vector Problem 1



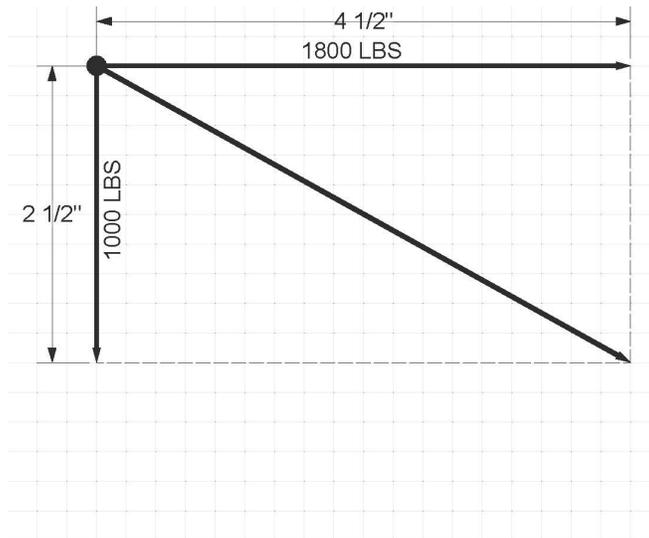
# Vector Problem 1



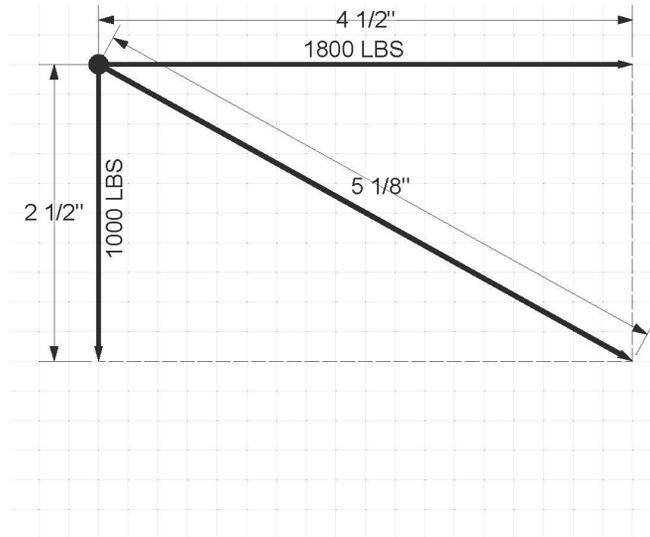
# Vector Problem 1



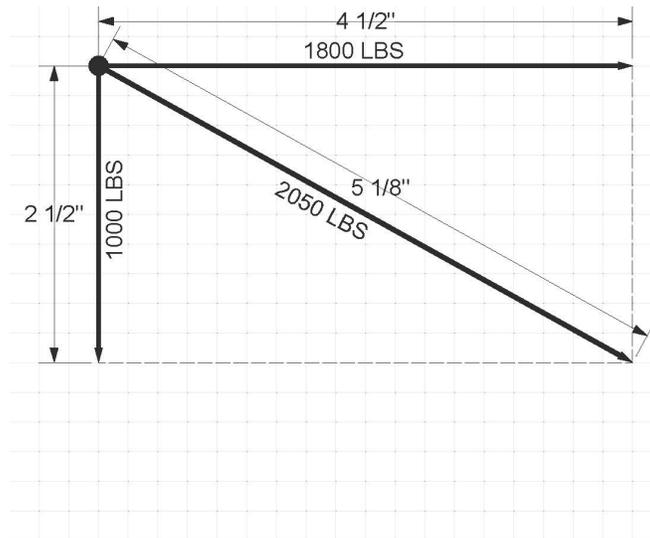
# Vector Problem 1



# Vector Problem 1



# Vector Problem 1



# Vector Problem 1

